

Equity, Welfare, and the Setting of Trade Policy in General Equilibrium[★]

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Abstract

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Key words: inequality, general equilibrium, trade, political economy of equity

JEL: F13, O15, D31, D72

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1 Introduction

In this paper, we develop a dual approach to analyzing general equilibrium relationships between trade policy and the household (as distinct from the functional) distribution of income. We follow Bourguignon and Morrisson [4], [5] and Spilimbergo *et al.* [27] and use an ownership matrix that allows us to move from functional to household income. We then obtain a dual representation of the household income distribution in terms of endowments, tariffs and the ownership structure. Using this analytical framework, we analyze the impact of trade and tariffs. Treating equity issues as relevant, we work with Sen [23] type social welfare functions and embed inequality indexes in social welfare functions. In particular, we work with the widely used Gini coefficient and with the Atkinson [2] family of inequality indexes, although other indexes may be employed. Using this framework we are able to decompose the general equilibrium import protection effects into real income level and dispersion changes.¹

Driven in large part by continued policy interest, the relationship between trade openness and wages has also been an active topic of debate in the research community.² However, this literature focuses on the functional distribution of income, with less emphasis on household distribution issues.³ The current literature has stressed theoretical linkages based on the Stolper-Samuelson theorem. In this context, tariff reductions in poor labor-abundant countries are expected to increase the real income of workers and hurt capital owners (or skilled labor). In developed countries the opposite effect is expected. The empirical evidence remains mixed and somewhat contradictory. The efficiency properties of tariffs are also well developed in the literature. What we highlight here is how general equilibrium distributional aspects of social welfare related to import protection may be examined alongside corresponding efficiency aspects in a dual framework. For government, this is manifested not only in special interest politics, but also through the direct impact of inequality on a government's objective function. We find that equity considerations may serve to counter lobbying interests in both capital-rich and capital-poor countries, though with an opposite marginal impact on the final policy outcome. Although we focus our attention on import tariffs, the main message that

¹ Also see Anderson [1]. While his paper is focused on a different set of issues (his goal is to explore the public finance concept of the marginal cost of funds in general equilibrium), he does stress the decomposition of general equilibrium welfare effects of raising public funds into a composition (i.e. efficiency) effect and a distributional effect.

² Comprehensive surveys are provided by Richardson [22], Cline [6] and Feenstra and Hanson [10].

³ Recent papers on this topic include Edwards [9], Higgins and Williamson [16], Barro [3] and Spilimbergo *et al.* [27].

follows from this approach can be applied in a more general context of trade policy instruments. The precise distributional and efficiency components may change, but in essence the trade-off and interrelation between both economic outcomes is still present.

The paper is organized as follows. Section 2 develops a formal representation of social welfare inclusive of income inequality. In Section 3, we embed this social welfare function into a dual general equilibrium trade model. We also develop the equilibrium representation of inequality, based on the dual representation of general equilibrium system fundamentals. Section 4 then explores linkages between trade policy, inequality, and welfare. It also examines theoretical linkages between country size, development, policy, and inequality. In Section 5, we explore the implications of the addition of inequality to the social welfare component of a government's objective function for political support function models of tariff formation. We conclude in Section 6.

2 Defining social welfare with respect to inequality

Our goal in this section is to develop a functional linkage between inequality and aggregate (social) welfare. This will then be integrated in the next section into a dual general equilibrium trade model. A critical condition for inequality to have a meaningful link to aggregate (social) welfare is that the utility function be strictly concave with respect to income. Additionally, for tractability we prefer to work with a social welfare function that is symmetric and additively separable in individual utilities.

The existence of social welfare functions depends crucially on the possibility to compare interpersonal utility levels. One such possibility is offered by the 'veil of ignorance' approach first proposed by Harsanyi [13], [14] and further developed by Rawls [21], where we rank different individual situations not knowing which would be the actual situation. As stated by Sen [25] this interpersonal comparison can be defined as those situations where we make judgements of the type:

"I would prefer to be person A rather than person B in this situation" and "while we do not really have the opportunity (or perhaps the misfortune, as the case may be) of in fact becoming A or B, we can think quite systematically about such a choice, and indeed we seem to make such comparisons frequently".

Because GDP per capita is the most common indicator of social welfare, the 'veil of ignorance' approach supports the use of an inequality measure to complement GDP per capita comparisons. If we do not know which individual

household we are in a specific country, then the expected utility becomes a function of mean income and the personal distribution of income. How we evaluate the probability of receiving any given income is then determined by the functional representation of the utility function and more specifically by the degree of concavity of this function. In this context, a natural extension of cross-country welfare comparisons is to complement GDP per capita levels with some measure of inequality.⁴

Under the social welfare approach to income distribution measurement, inequality is associated with variance in the distribution of income. This raises two measurement problems. The first is that we cannot generally rely on first moment-based indicators. The second is that even though the concepts of Lorenz-dominance and general Lorenz-dominance (Shorrocks [26]) are accepted as ways to impartially rank two different distributions⁵, in many cases the Lorenz-curves intersect at least once, so that we obtain incomplete ranking of distributions. To solve both these problems, inequality indexes are usually used to rank distributions in indeterminate cases and to provide a summary variable that can be used in empirical models. While the most commonly used is the Gini coefficient, most inequality measures are implicitly based on a social welfare function (Dalton [7]; Kolm [18]; Atkinson [2]). As such, there is no perfect index, and any index has built in social preferences.

In this paper, we employ two representations of household utility and social welfare. Both reflect Sen's [23] preferred definition of social welfare as:

$$SW = \bar{y}(1 - I) \tag{1}$$

where SW is the social welfare, \bar{y} is mean income, and I is an index of inequality.

Starting with CRRA preferences yields the well-known Atkinson inequality index directly as a natural metric for a mapping from income distribution to social welfare (see Atkinson [2]). In this sense, Atkinson's index fits naturally into Sen's proposed social welfare function.

Sen actually offered equation (1) as defined with respect to the Gini coefficient. In this case, the social welfare function is axiomatic, in that we do not have an obvious mapping –through aggregation– from individual preferences to an aggregate social welfare function. This follows because the social welfare function is then rank sensitive. We work with both the Atkinson index and Gini coefficient in this paper.

⁴ This approach was formally treated by Sen [24].

⁵ See Lambert [19] for details.

2.1 The Atkinson index-based social welfare function

Formally, we define a composite consumer good over the range of all consumption goods, which follows from a linear homothetic aggregation function. As such, cost minimization yields a composite consumer price index. This is defined over all consumer prices p_c .

$$p_c = f(p) \tag{2}$$

Household utility u^h is defined as a function of household consumption of the composite consumer good c^h :

$$u^h = \psi(c^h) \tag{3}$$

We next map aggregate individual utility to aggregate welfare ϕ , which is defined as the sum of household utility,

$$\phi = \sum_h u^h \tag{4}$$

while aggregate consumption c is the sum of household consumption.

$$c = \sum_h c^h \tag{5}$$

We will assume that the function ψ is CRRA:⁶

$$\psi(c^h) = \begin{cases} \frac{(c^h)^{1-\theta}}{1-\theta} & \text{if } \theta \neq 1 \\ \ln c^h & \text{if } \theta = 1 \end{cases} \tag{6}$$

In general, we assume that $\theta > 0$, and in this paper we focus on the case where $\theta \neq 1$.⁷ We employ a simple linear transformation, and are then able to define a social welfare index in per-capita terms.

⁶ In the present context, constant relative inequality aversion (CRIA) is a better label and acronym.

⁷ One gets the same basic results with log preferences. Estimates in the macro literature are that θ is less than 1.

$$SW_A = (1 - \theta) n^{-1} \sum \psi = \frac{1}{n} \sum_h (c^h)^{1-\theta} \quad (7)$$

Simple manipulation then yields social welfare as a function of per-capita income \bar{y} , consumer prices, and income equality.

$$SW_A = \left(\frac{\bar{y}}{p_c} \right)^{1-\theta} E_A \quad (8)$$

With some further manipulation, our equality measure E_A can be mapped directly to the Atkinson index of income inequality, yielding a Sen-type social welfare function. In particular, taking the definition of the Atkinson index, we have the following relationships between the Atkinson index I_A , E_A , and social welfare.

$$I_A = 1 - \left(\frac{1}{n} \sum_h \left(\frac{y^h}{\bar{y}} \right)^{1-\theta} \right)^{\frac{1}{1-\theta}} = 1 - E_A^{\frac{1}{1-\theta}} \quad (9)$$

$$SW_A = \left[\left(\frac{\bar{y}}{p_c} \right) (1 - I_A) \right]^{1-\theta} \quad (10)$$

Note that as $\theta \rightarrow 0$ only average income matters, rather than income inequality. Alternatively, when $\theta \rightarrow \infty$, then $SW_A = \min(y^h)$ and we have the extreme Rawlsian maximin social welfare function, where the income level of the poorest individual is the only relevant variable and average income is unimportant. Moreover, for a given distribution (measured as shares of total income) we have declining marginal utility of income.

2.2 The Gini index-based social welfare function

The Gini coefficient is defined as twice the area between the Lorenz curve and the 45-degree line. As such, $(1 - G)$ is then twice the area below the Lorenz curve. Formally, this index is defined as follows:

$$I_G = 1 + \frac{1}{n} - \frac{2}{n^2 \bar{y}} (y^1 + 2y^2 + \dots + ny^n) = 1 + \frac{1}{n} - \left[\left(\frac{2}{n^2} \sum_h \frac{hy^h}{\bar{y}} \right) \right] \quad (11)$$

$$SW_G = \left[\left(\frac{\bar{y}}{p_c} \right) (1 - I_G) \right] \quad (12)$$

where we have arranged households so that $y^1 \geq y^2 \geq \dots \geq y^n$. Unlike the Atkinson-based social welfare function, the Gini-based social welfare function embodies asymmetry not on specific individuals, but rather on relative income rankings. This ranking provides the concavity of the utility function with respect to income. The higher the income in the ranking, the less social weight it has. At the same time, equation (12) is linear in average income. As such, SW_G is relatively more sensitive to mean income than SW_A and less sensitive to inequality.

3 Inequality and trade in general equilibrium

To explore the interaction between production, trade and trade policy, and inequality, we work with a modified dual representation of trade in general equilibrium (Dixit and Norman [8]). To do so, we first adopt the following additional set of assumptions:

- Rational behavior by households and firms.
- Complete and perfectly competitive markets.
- Convex technology, with neoclassical production functions.
- Goods are tradable and factors are not.
- Every household has the same neoclassical technology for producing the composite consumption good.

Given these assumptions, we are able to define the core general equilibrium system for demand and production in terms of expenditure and revenue functions, with expenditure defined in terms of the composite consumption good. Social welfare then follows as a set of side equations from the core general equilibrium system.

3.1 *The core general equilibrium system*

Because we assume that all households have the same consumption technology defined with respect to the composite consumption good, we can drop the household index from consumption and represent aggregate expenditure as a function of aggregate consumption and prices:

$$e(p, c) = c \cdot f(p) \quad (13)$$

On the production side, we assume standard neoclassical production functions with constant returns to scale: $x_i = g_i(v_{ji})$, where $g_i(\cdot)$ is the production function for good i and v_{ji} is the use of factor j in the production of good i . Defining unit input coefficients as a_{ji} we also obtain: $1 \leq g_i(a_{ji})$. Endowment constraints are then $\sum a_{ji}x_i \leq \bar{v}_j$. From these conditions, we can define the economy-wide revenue function with respect to goods prices and endowments. This is represented in equation (14).

$$r(p, v) = \max_{x_i, a_{ji}} \left\{ \sum_i p_i x_i \mid \sum_i a_{ji} x_i \leq \bar{v}_j \text{ and } 1 \leq g_i(a_{ji}) \quad \forall i, j \right\} \quad (14)$$

From the envelope theorem and the properties of the revenue function r , factor incomes and goods production can be expressed in terms of the value of the partial derivatives of the revenue function, evaluated at the equilibrium set of prices:

$$\frac{\partial r(p, v)}{\partial v_j} = w_j = w_j(p, v) \quad \forall j \quad (15)$$

$$\frac{\partial r(p, v)}{\partial p_i} = x_i = x_i(p, v) \quad \forall i \quad (16)$$

Taking equations (15) and (16) in conjunction with equations (13) and (14), we can write the general equilibrium system for production, consumption, and trade as follows:⁸

$$c^h f(p) = \left(\sum_j w_j(p, v) \cdot v_j^h \right) + \omega_\tau^h \tau m \quad \forall h \quad (17)$$

$$m = \sum_h c^h \cdot f(p) - x(p, v) \quad (18)$$

$$e(p, c) = \sum_h \left[\left(\sum_j w_j(p, v) \cdot v_j^h \right) + \omega_\tau^h \tau m \right] \quad (19)$$

$$p = P^* + \tau = 1 + \tau \quad (20)$$

In equations (17) – (20), we have assumed the home country imposes a tariff of τ on imports from the rest of the world, while world prices are normalized to one. In addition, ω_t^h is the household share of the tariff revenue and v_j^h is the household ownership share of factor j . In the first equation, household

⁸ A two-country general equilibrium system can readily be formalized using the same framework.

consumption is equal to the household budget. Equation (18) defines imports on which tariff revenue is generated and equation (19) sets economy wide expenditure equal to national income. Together, the system of four equations has an equally dimensioned set of unknowns: c^h, m, e and p .

3.2 Household inequality

As explained earlier, the recent literature on trade and the distribution of income has focused on the functional distribution of income. The functional distribution of income is also an important building block here for the representation of the household distribution of income. In equation (21) we define factor incomes s , which follow directly from the endowment stock and the properties of the revenue function.

$$s_j = r_{vj}(p, v) \cdot v_j = w_j v_j \quad (21)$$

Thus, the functional distribution of income is a function of equilibrium prices, preferences, the production technology and the endowment set. In reduced form, the functional distribution of income $F(s)$ is then an artifact of the equilibrium matching of preference and the technology set, given our endowment vector.

$$F(s) = F(p, v) \quad (22)$$

Using factor incomes w_j and the household ownership share of production factors, ω_j^h we can readily obtain household income. In addition, we include the assignment of import tariff revenue, again represented by a household share parameter. Equation (23) presents the basic definition of household income in terms of its primary components.

$$y^h = \left(\sum_j w_j \cdot v_j \cdot \omega_j^h \right) + \omega_\tau^h \tau m \quad (23)$$

$$c^h = \frac{y^h}{p_c} \quad (24)$$

where $1 \geq \omega^h \geq 0$ and $\sum \omega_j^h = \sum \omega_\tau^h = 1$. In reduced form, the personal distribution of income $F(y)$ is a consequence of the elements affecting the functional distribution and the $h \times j$ ownership matrix of coefficients ω_j^h , represented by Ω :

$$F(y) = F(p, v, \Omega) \quad (25)$$

Note that social welfare is ultimately a function of the ownership matrix in the economy, while the impact of trade policy will then depend on the interaction of the underlying economic structure and the ownership matrix.

3.3 Inequality indexes with system fundamentals

We can write our social metrics of the distribution of income –the Atkinson and Gini indexes– in terms of system fundamentals. Making a substitution from (23) into (9) and (11), we obtain the following equations:

$$I_A = 1 - \left\{ \frac{1}{n} \sum_h \left[\frac{n \left(\sum_j w_j v_j \omega_j^h \right) + n \omega_\tau^h \tau m}{y} \right]^{1-\theta} \right\}^{\frac{1}{1-\theta}}$$

$$I_A = 1 - \left\{ n^{-\theta} \sum_h \left[n^{-1} + \sum_j \beta_j \left(\omega_j^h - n^{-1} \right) \right]^{1-\theta} \right\}^{\frac{1}{1-\theta}} \quad (26)$$

$$I_G = 1 + \frac{1}{n} - \frac{2}{n^2} \sum_h h \left[\frac{n \left(\sum_j w_j v_j \omega_j^h \right) + n \omega_\tau^h \tau m}{y} \right]$$

$$I_G = 1 + \frac{1}{n} - \frac{2}{n} \sum_h h \left[n^{-1} + \sum_j \beta_j \left(\omega_j^h - n^{-1} \right) \right] \quad (27)$$

where $\beta_j = \frac{w_j v_j}{y}$ represents the national income share of factor j and $\sum_j \beta_j + \frac{\tau m}{y} = 1$. In what follows, we apply the additional normalization that each household receives an equal share of the tariff revenues, so that $\omega_\tau^h = n^{-1}$.⁹

The ratio of the household's income to per capita income, which accounts for income dispersion, is given by the sum of the differences between the actual ownership share of factors and equal shares for each household. From equations (26) and (27), we can make a substitution back into equations (10) and (12), yielding social welfare itself as a function of system fundamentals.

⁹ The distributional impact of tariff revenues can be substantial. This is the emphasis of the paper by Galor [11], which includes tariffs in his general equilibrium Overlapping-Generations model.

$$\begin{aligned}
SW_A &= \left[\frac{\bar{y}}{p_c} (1 - I_A) \right]^{1-\theta} \\
SW_A &= \left(\frac{\bar{y}}{p_c} \right)^{1-\theta} n^{-\theta} \sum_h \left[n^{-1} + \sum_j \beta_j (\omega_j^h - n^{-1}) \right]^{1-\theta}
\end{aligned} \tag{28}$$

$$\begin{aligned}
SW_G &= \frac{\bar{y}}{p_c} (1 - I_G) \\
SW_G &= \left(\frac{\bar{y}}{p_c} \right) \left\{ \frac{2}{n} \sum_h h \left[n^{-1} + \sum_j \beta_j (\omega_j^h - n^{-1}) \right] - n^{-1} \right\}
\end{aligned} \tag{29}$$

4 Trade policy, distribution, and welfare

From equations (28) and (29) above, social welfare is a function of the first two moments of the household distribution of income. This is especially obvious with the Atkinson index, as it is actually the weighted variance of income, with inverse income weights, that provides the variance component of the social welfare function.¹⁰ Because the contributions of the mean and variance components of income to social welfare are separable in equations (28) and (29), we can decompose the impact of trade policy as well into its impact on per-capita income (an efficiency effect), and its impact on the variance of income (a distributional effect). Together, they determine the overall social welfare impact. Formally, differentiating equations (28) and (29) with respect to tariffs, we obtain the following equations:

$$\begin{aligned}
\frac{\partial SW_A}{\partial \tau} &= (1 - \theta) \left[\frac{\bar{y}}{p_c} (1 - I_A) \right]^{-\theta} (1 - I_A)^{1-\theta} \left(\frac{\partial \bar{y}}{\partial \tau} - \frac{\partial p_c}{\partial \tau} \frac{\bar{y}}{p_c^2} \right) \\
&\quad - (1 - \theta) \left(\frac{\bar{y}}{p_c} \right)^{1-\theta} I_A^{-\theta} \frac{\partial I_A}{\partial \tau}
\end{aligned} \tag{30}$$

$$\frac{\partial SW_G}{\partial \tau} = (1 - I_G) \left[\frac{\partial \bar{y}}{\partial \tau} - \frac{\partial p_c}{\partial \tau} \frac{\bar{y}}{p_c^2} \right] - \left(\frac{\bar{y}}{p_c} \right) \frac{\partial I_G}{\partial \tau} \tag{31}$$

How do we interpret equations (30) and (31)? The efficiency component is well known (see for example Dixit and Norman [8].), and is shown here in equation

¹⁰ While the functional form is different, the social welfare function underlying other income distribution indexes yields a similar result, though with different weights in the variance component of the welfare function. The CRRA function yields a particularly clear and parsimonious reduced form.

(32). Basically, the impact of the tariff on per-capita income will depend on the combination of terms-of-trade and allocation effects (the first set of terms in square brackets in equation (32)), and tariff revenue (the second set of terms).

$$\frac{\partial \bar{y}}{\partial \tau} = \frac{1}{n} \sum_h \frac{\partial y^h}{\partial \tau} = \frac{1}{n} \left[m \left(1 - \frac{\partial p}{\partial \tau} \right) + \tau \frac{\partial m}{\partial \tau} \right] \quad (32)$$

For a small country, negative allocation effects outweigh the terms-of-trade effects, so that the impact of the tariff on mean income is strictly negative. Also, for the small country, the impact on the cost of living will be to raise prices. As such, the real mean-income effect will be strictly negative for a small country. With a large country, the combined income and cost-of-living effect, or in other words the real income effect of the tariff change as represented by the term in square brackets in the equations (30) and (31) may be positive or negative depending on the magnitude of terms-of-trade effects.

The impact on household income distribution, the other part of equations (30) and (31), follows from differentiation of equations (26) and (27). This is shown below:

$$\begin{aligned} \frac{\partial I_A}{\partial \tau} = & -n^{\frac{-\theta}{1-\theta}} \left\{ \sum_h \left[\sum_j \beta_j (\omega_j^h - n^{-1}) + n^{-1} \right]^{1-\theta} \right\}^{\frac{\theta}{1-\theta}} \\ & \sum_h \left\{ \left[\sum_j \beta_j (\omega_j^h - n^{-1}) + n^{-1} \right]^{-\theta} \left[\sum_j \frac{\partial \beta_j}{\partial \tau} (\omega_j^h - n^{-1}) \right] \right\} \end{aligned} \quad (33)$$

$$\frac{\partial I_G}{\partial \tau} = -\frac{2}{n} \sum_h h \left[\sum_j \frac{\partial \beta_j}{\partial \tau} (\omega_j^h - n^{-1}) \right] \quad (34)$$

Note that we also have an inverse income weighting, by a factor of θ , in equation (33) applied to induced changes in income. The weighting of induced changes in income for the Gini index depends on the ranking of individual households on the relative income scale.

Close inspection of equations (33) and (34) reveals a more general relationship between inequality and tariffs. In particular, if we define ethical weights ψ , then for a broad class of inequality measures, we will have

$$\frac{dI}{d\tau} = \sum_h \psi^h \left[\sum_j \frac{\partial \beta_j}{\partial \tau} (\omega_j^h - n^{-1}) \right] \quad (35)$$

In this context, assuming we adopt a Sen-type social welfare function (where we also allow for a marginal utility of income coefficient α) so that our ethical weights ψ map to an index of equity E , we then also have:

$$SW = \left[\left(\frac{\bar{y}}{p_c} \right) [1 - I] \right]^\alpha \quad (36)$$

$$\frac{\partial SW}{\partial \tau} = \alpha \left[\left(\frac{\bar{y}}{p_c} \right) [1 - I] \right]^{\alpha-1} \left([1 - I] \left(\frac{\partial \bar{y}}{\partial \tau} p_c^{-1} - \frac{\partial p_c}{\partial \tau} \frac{\bar{y}}{p_c^2} \right) - \left(\frac{\bar{y}}{p_c} \right) \sum_h \psi^h \left[\sum_j \frac{\partial \beta_j}{\partial \tau} (\omega_j^h - n^{-1}) \right] \right) \quad (37)$$

In general, changes in household income depend on the set of factor price changes, filtered by the ownership matrix and our ethical weights, where factor price changes in turn depend on Stolper-Samuelson derivatives and the induced price changes that follow from tariff changes. This is expressed in equation (38), where the term $\frac{\partial \beta_j}{\partial \tau}$ depends on system fundamentals and Stolper-Samuelson relationships.

$$\frac{\partial \beta_j}{\partial \tau} = \frac{\partial w_j}{\partial p} \frac{\partial p}{\partial \tau} \frac{v_j}{y} - \frac{\partial y}{\partial \tau} \frac{w_j v_j}{y^2} \quad (38)$$

We can also represent the relationship in elasticity terms: $\varepsilon_{\beta_j, \tau} = \varepsilon_{w_j, p} \varepsilon_{p, \tau} - \varepsilon_{y, \tau}$.

4.1 Social Welfare with Inequality in the 2x2 Model

Assuming that inequality is the result of uneven distribution of an asset that is indexed by k , we can apply equation (35) to a two-factor, two-good Heckscher-Ohlin model. In this framework, equation (39) determines the impact of tariff changes on household inequality.

$$\frac{\partial I}{\partial \tau} = \sum_h \psi^h \left[\frac{\partial \beta_k}{\partial \tau} (\omega_k^h - n^{-1}) \right] \quad (39)$$

Inequality is purely a function of the allocation of assets in this model. At the same time, the impact of the tariff is then a function of which sector is protected. If protection leads to a drop in asset income, inequality is reduced. Alternatively, if asset income is protected, we will see a rise in inequality. Note that our discussion in terms of assets includes both the 2x2 capital-labor and 2x2 skilled-unskilled versions of the Heckscher-Ohlin model found in the literature on the functional distribution of income. The interpretation of β_k

with physical capital is obvious. If we instead are working with skilled and unskilled labor in the 2x2 model, then the return to skill as an asset will be $\beta_k = [\beta_s - n_s n^{-1} \beta_u]$ where β_s is the income share of skilled labor, interpreted as including both the basic labor and skill component of skilled labor income, and where s and u index skilled and unskilled workers.¹¹ Substituting skill for capital, we will arrive at equation (39).

While inequality depends on relative factor incomes, the social welfare effect will depend on the trade-off between real income effects following from import protection, and the impact on inequality. In other words, the trade-off between equity and efficiency. From equations (36) and (37), this is ultimately a function of the degree of inequality aversion, combined with the structural features of the economy and its market power on world markets. For a small country, real income effects will be strictly negative, while inequality effects may be positive or negative, depending on the relative endowment structure of the economy. For a large country, it is possible for both effects to work in the same direction. However, in this case, note that positive terms-of-trade gains will slow any rise (or slow any fall) in capital income shares, from equation (38). This in turn means that terms of trade effects will tend to mitigate the inequality effects of protection.

On the basis of equations (38) and (39), we can summarize our discussion above with the following observations about import protection and inequality in the 2x2 Heckscher-Ohlin model.

Observation 1 *In a small 2x2 economy with inequality determined by uneven distribution of assets (capital or skill), tariffs will cause inequality to rise (fall) if assets in the economy are relatively scarce (abundant).*

If we take the factor in the 2x2 model that is unevenly distributed as assets (capital or skill), then from equation (39), changes in inequality indexes depend strictly on a weighted sum of the change in the share of income going to those assets, $\frac{\partial \beta_k}{\partial \tau}$. From the Stolper-Samuelson theorem, the income share of those assets will rise (fall) with a tariff if the economy is asset poor (rich). Weights are assigned to households that are inversely monotonic in household capital deviations from the average, $(\omega_k^h - n^{-1})$ in both the Atkinson and the Gini case. This means that the change in incomes for households holding more

¹¹ Formally, assume first that unskilled labor earns w_u and skilled labor earns w_s , where $w_u < w_s$. We can then decompose the skilled labor price into two components, such that $w_s = w_u + (w_s - w_u)$. If we define skill as an asset with return r_k , then we can now define $r_k = (w_s - w_u)$. Viewed this way, all households have been endowed with a claim on income equal to the price of a unit of basic labor earning w_u , while some have also been endowed with a claim on the income of a unit of skill. The distribution of this claim on skill income is then the source of inequality. In share terms, we will have $\beta_s = n_s n_u^{-1} \beta_u + \beta_k$, or, $\beta_k = \beta_s - n_s n_u^{-1} \beta_u$.

capital than average or households holding skilled labor, and hence more income than average, determine the sign of the income effect. As a result we will have a rise (fall) in equality as a capital poor (rich) country imposes a tariff.

On the basis of Observation 1 we can immediately make the following statements about asset rich and poor Heckscher-Ohlin economies.

Corollary 1 *In a small asset-poor Heckscher-Ohlin economy, where the mean real-income effects of import protection are negative, we have a magnification effect. The effect of import protection on welfare through mean income is magnified by the impact through inequality. Because of this magnification effect, net effects remain unambiguous and negative.*

Corollary 2 *In a small, asset-rich Heckscher-Ohlin economy, where the mean real-income effects of import protection are negative, we have a mitigation effect. The effect of import protection on welfare through mean income is at least partially offset by the impact through inequality. From Observation 1 and equations (30) and (31) the net welfare effect is ambiguous. It depends on the specification and parameterization of the underlying social welfare function.*

Corollary 3 *The impact of protection on inequality as measured by the Atkinson and Gini indexes will be weaker, in a Heckscher-Ohlin economy, for large countries. This is because of terms of trade effects from equation (38), which will dampen the goods-price to factor-price transmission mechanisms at play.*

Corollary 1 flags a magnification effect, linking efficiency and inequality effects, in labour abundant economies. In contrast, we instead have an offsetting effect in capital-abundant economies, as noted in Corollary 2. This result means that, in the 2x2 model, the impact of tariffs on welfare can be ambiguous for small economies when inequality matters. This stands in contrast to a standard result of the classic 2x2 model, where tariffs are unambiguously welfare-reducing for small countries. Corollary 3 follows because our tariff analytics are driven by the transmission of tariff changes into price changes, and these are weaker in larger economies. These smaller internal price effects mean smaller inequality effects.

4.2 Social Welfare with Inequality in the Specific Factors Model

Next, consider the specific factors model. We can make a similar manipulation of equation (35), yielding equation (39), for the standard 2-good, 3-factor model. This yields equation (40) below. Again, if we assume that inequality follows from the ownership pattern of (specific) assets (ki), then in this case a shift in income shares through protection from more to less concentrated factors (in terms of the concentration of factor ownership) yields a reduction in

inequality. The same points then follow, as before, with regard to country size and inequality effects in the Heckscher-Ohlin model. Otherwise, the impact of protection on inequality depends on the pattern of relative factor prices and ownership effects.

$$\frac{\partial I}{\partial \tau} = \sum_h \psi^h \left[\frac{\partial \beta_{k1}}{\partial \tau} (\omega_{k1}^h - n^{-1}) + \frac{\partial \beta_{k2}}{\partial \tau} (\omega_{k2}^h - n^{-1}) \right] \quad (40)$$

We can summarize our results with respect to the Ricardo-Viner model as follows:

Observation 2 *In a small 2x3 Ricardo-Viner economy, with inequality determined by uneven distribution of both specific factors, if assets represent shares in the combined portfolio of specific capital, tariffs will cause inequality to fall if the collective income share of both specific factors falls, implying also that the share for the mobile factor will also rise.*

From equation (40), changes in inequality indexes depend strictly on a weighted sum of the change in the share of income going to both forms of sector-specific assets, $\frac{\partial \beta_{ki}}{\partial \tau}$. Weights are assigned to households that are inversely monotonic in household deviations from the average portfolio, $(\omega_{ki}^h - n^{-1})$. This means that the change in incomes for households holding more assets than average, and hence more income than average, determine the sign of the income effect. As a result we will have a fall in inequality as long as all asset income shares decline.

Observation 3 *Unless the conditions in Observation 2 are met, the impact of protection on inequality as measured by the Gini or Atkinson index, like the impact of a tariff on income for the mobile factor itself, is ambiguous in the Ricardo-Viner model when specific factor ownership patterns are the source of inequality.*

Observation 3 follows from the need to sign the final terms in square brackets in equation (40). In the special case covered by Observation 2, we can unambiguously make a statement about inequality. In the more general case however, we can generate examples where the tariff-induced changes in the specific-factor share of income may vary in sign between the two sectors. Depending on the distribution of ownership, functional forms, and the share of unskilled labor in total income in the benchmark, inequality may then rise or fall. For example, in a developing country where the poor have unskilled labor and land, and the rich unskilled labor and capital, protection will make the concentration of income worse, assuming the sector using capital is an import-competing sector. On the other hand, if ownership of land is very highly concentrated relative to capital, import protection may improve the distribution of income.

Following from Observation 3 and equations (30) and (31), we can state that in the standard 2x3 model, if the induced change in inequality is large enough and of the correct sign, it can offset the impact of the change in average income levels. This all depends on the underlying functional forms in the model and the parameterization of the social welfare function. If inequality is not improved, then the worsening inequality magnifies the negative efficiency effects of small-country tariff incidence. This is summarized as follows.

Corollary 4 *In a small Ricardo-Viner country, import protection may be welfare improving even though average incomes will fall.*

5 The Setting of Trade Policy

At this point, we could invoke a variety of different political economy models to generate political underpinnings for the setting of an equilibrium tariff in the political marketplace. These models have been extensively analyzed in the recent literature¹², and following Helpman [15] we note that many of these can be represented, in reduced form, by the now standard political support function.

Direct democracy is a rare political mechanism and public policies are more usually decided by representative governments that balance conflicting interests. From Hillman [17] we know that when one of the factors is sufficiently concentrated across only a few households, these individuals can organize to form pressure groups and overcome the free-rider problem. In such cases, Grossman and Helpman have demonstrated that in the reduced form the policy maker has two arguments to consider: the general interest and the interest of special groups (for example capital owners and unions). The interest of the government can follow from electoral support when social welfare is increasing and electoral contributions go with lobbying. For example, in the 2x2 model, investors in a poor labor-abundant country can offer a contribution to induce the policy-maker to increase import protection.

The precise weight the policy maker assigns to each group is established by her political support function, as in equation (41).

$$U(\tau) = \lambda_1 SW(\tau) + \lambda_2 \rho(\tau) \quad (41)$$

where U is the policy-maker's utility, ρ represents (lobbying) rents generated for government through protection, and where we assume that the tariff level is

¹² See for example Helpman [15] and Grossman and Helpman [12].

the only policy instrument of the government. The weights λ characterize the political system (how important are the contributions for the electoral campaign) and the policy-makers' preferences (how she values reelection against more contributions).

Conditional on the particular values of these weights, she maximizes her utility by the first order condition shown in equation (42).

$$\frac{\partial U(\tau)}{\partial \tau} = \lambda_1 \frac{\partial SW(\tau)}{\partial \tau} + \lambda_2 \frac{\partial \rho(\tau)}{\partial \tau} = 0 \quad (42)$$

where $\frac{\partial SW(\tau)}{\partial \tau}$ has been already defined in equations (36) and (37). Since ρ is the fraction of the capital/asset rents that are assigned to political contributions, $\frac{\partial \rho(\tau)}{\partial \tau} > 0$ until the optimum tariff for investors is reached. (Mayer [20])

The additional element in the political mixture here is the effect of the tariff on social welfare through inequality, $\left(\frac{\partial I(\tau)}{\partial \tau}\right)$. From equations (36) and (37) the tariff impact on an inequality-adjusted social welfare function can induce changes to the standard results of the political support model. Thus, there is not necessarily a trade-off between both right hand side terms in equation (41) and in some cases they can reinforce each other.

If we analyze small open economies and consider only the social welfare implications (or identically where $\lambda_2 = 0$), when the distributional effect of the tariff compensates for more than the efficiency losses incurred we will observe a positive optimum tariff rate. From Corollary 2, in the 2x2 case this can be the case only for capital-abundant countries. On the other hand, from Corollary 1, in poor 2x2 countries the distributional and efficiency effects reinforce each other and the socially optimum tariff is zero, though the equilibrium rate may be positive when $\lambda_2 > 0$. In a specific factors setting (see below) things are less clear-cut.

When the influence of special interest groups is introduced, the previous partial results can change. In a capital-abundant 2x2 country, the capital-owners have an incentive to lower tariffs, and if the workers can organize, they lobby to increase tariffs. The final outcome depends on the specific rents each group obtains and its political influence. In labor-abundant 2x2 countries positive tariffs can be explained by the presence of an effective lobby, and in capital rich countries they can be explained by equity concerns that partially overcome free trade lobbying.

These multiple outcomes are summarized as follows:

Observation 4 *In a Heckscher-Ohlin world, with homogeneous labor owners,*

concentrated capital and a policy-maker that cares about equity and assigns no weight to political contributions, the government's optimum tariff is higher in capital-abundant countries than in labor-abundant countries.

From Observation 1, tariffs will lead to a rise (fall) in inequality depending on whether a country is capital rich (poor). In conjunction with equations (28) and (29), this means that tariffs have a positive (negative) impact on welfare, all other things equal, in capital rich (poor) countries mapped through inequality effects. Hence tariffs are better than represented by mean effects alone in rich countries, and worse than in poor countries. So the government's optimum tariff is then higher in capital-abundant countries than in labor-abundant countries.

Starting from Observation 4, once we introduce a non-zero weight for lobbyists ($\lambda_2 > 0$) we can then have the following corollaries.

Corollary 5 *In a Heckscher-Ohlin capital-abundant economy, with relatively greater inequality aversion, while capital owners will lobby for lower tariffs, the government will be relatively more protectionist because of equity reasons than otherwise. Equity concerns then offset to some extent pressure for lower tariffs in the political marketplace.*

Corollary 6 *In a Heckscher-Ohlin labor-abundant economy, with relatively greater inequality aversion, the government will favor relatively lower tariffs for equity and efficiency reasons, but will be lobbied by capitalists for higher tariffs. Equity concerns then offset to some extent pressure for higher tariffs in the political marketplace.*

Basically, when the distributional effects are not significant enough to upset the efficiency losses imposed by the tariff, the common results of the literature emerge and higher tariffs are directly associated to the weight and the contributions of special interest groups. At the same time though, in the presence of distributional concerns rich countries tend to impose higher tariffs than otherwise. Relatively high average tariffs across a subset of capital-rich countries can then be seen as a consequence of greater inequality considerations by the relevant policy-makers, as well as the presence of influential unions. In poor countries positive tariff rates are a direct consequence of the investor lobby overcoming both equity and efficiency concerns of the government. In developing countries with a political system that assigns a significantly higher weight to social welfare than average, tariffs should remain lower than otherwise.

A similar analytical exercise can be carried out with a 2x3 specific-factors model. In particular, ignoring equity concerns, we have an equilibrium tariff that balances the efficiency effects of the tariff against the interests of owners of sector 1 and sector 2 capital. However, unlike the results for the Heckscher-Ohlin model we developed here, we will not then have unambiguous results

when we add inequality to the policy objective mix. This is because, from Observation 3, the inequality impact of a tariff may itself be ambiguous. If a tariff reduces inequality in the region of the political equilibrium, we would again expect the equity-conscious government to be more protectionist than otherwise. If not, we expect the opposite to hold. Like real wage effects, inequality effects also prove ambiguous in the 3x2 model, so that functional forms and parameters (or in the real world: preferences, technologies and endowments) all need to be given weight before an answer can be given.

6 Conclusions

We have developed a dual theoretical framework for exploring linkages between import protection and the household distribution of income. This complements the existing literature that links trade policy to factor incomes and the functional distribution of income, which is well developed in the literature. The main insight of this literature is provided by the Stolper-Samuelson theorem and constitutes a first step in our analysis. In a general equilibrium context, tariff changes ultimately affect the household distribution through variations in ownership patterns in conjunction with Stolper-Samuelson effects. To model ownership structures, we used the Heckscher-Ohlin and Ricardo-Viner trade models. Within both frameworks, we are then able to produce theoretical predictions between trade protection, country size, level of development, and personal income inequality.

Another contribution of this paper is that we examine the formal link between social welfare and the equilibrium determinants of the distribution of income. Using Sen-type social welfare functions, we decompose the general equilibrium welfare effects of import protection into real income level and distribution components. Depending on the representation of risk/inequality aversion, the dispersion component can be represented exactly through use of the Gini or Atkinson inequality indexes. With these explicit inequality derivatives we map import protection to inequality-adjusted welfare. In addition, when standard trade models are employed this framework also yields predictions relating social welfare with protection, country size and levels of development. In conjunction with the relevant inequality index, the general form of the decomposition of welfare and inequality we develop here may also be useful for producing summary measures of distributional impacts in applied general equilibrium applications focused on inequality.

Once the distributional effects of trade liberalization are determined, we can apply endogenous tariff formation models to assess how the optimum tariff is affected by equity concerns. In representative democratic systems, we find that positive optimum tariffs can be sustained in capital-abundant countries

even when the policy-maker assigns a low or zero weight to the contributions of special interests groups. In this case, the positive distributional effect of import protection can offset or compensate the efficiency losses of reduced trade. In poor countries, characterized by the relative abundance of labor, positive tariffs are explained by the influence of special interest groups (i.e. capitalists) that heavily lobby for higher tariffs. Thus, import protection in developing countries not only diminishes social welfare through efficiency and equity considerations, but also signals the economic and political weight of the capital-owners.

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